

$$d) \lim_{x \rightarrow \infty} \left(1 + \frac{a}{x}\right)^x = \lim_{x \rightarrow \infty} f(x) \quad \left| \ln[f(x)] = x \ln\left(1 + \frac{a}{x}\right)\right.$$

$$\lim_{x \rightarrow \infty} \ln[f(x)] = \lim_{x \rightarrow \infty} \frac{\ln\left(1 + \frac{a}{x}\right)}{\frac{1}{x}} = \lim_{x \rightarrow \infty} \frac{1}{1 + \frac{a}{x}} \cdot \left(\frac{-a}{x^2}\right) = a$$

$$\lim_{x \rightarrow \infty} f(x) = \lim_{x \rightarrow \infty} e^{\ln[f(x)]} = e^a$$

$$e) \lim_{x \rightarrow 1} x^{\frac{1}{x-1}} \quad \left| \ln[f(x)] = \frac{1}{x-1} \ln(x)\right.$$

$$\lim_{x \rightarrow 1} \frac{\ln(x)}{x-1} = \lim_{x \rightarrow 1} \frac{\frac{1}{x}}{1} = 1$$

$$\lim_{x \rightarrow 1} e^{\ln[f(x)]} = e^1 = e$$